

Given $f(x) = 3e^{x-5} + 4$, find $f^{-1}(x)$.

- To find the inverse of $y = f(x)$ we let $x = f(y)$ and solve for y .
- $x = 3e^{y-5} + 4$
- $x - 4 = 3e^{y-5}$
- $\frac{x-4}{3} = e^{y-5}$
- $\ln \frac{x-4}{3} = \ln(e^{y-5}) = y-5$
- $y = 5 + \ln \frac{x-4}{3}$ and $f^{-1}(x) = 5 + \ln \frac{x-4}{3}$