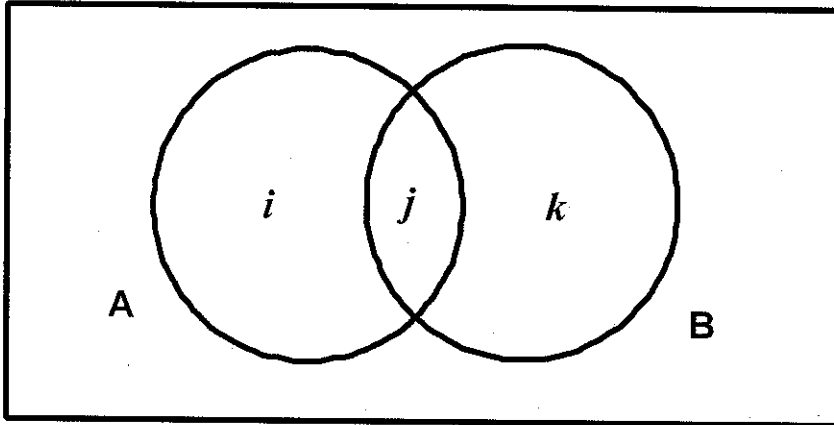


# GENERAL ADDITION RULE

Outcome Space



*n* equally likely outcomes

$$\text{Probability of } A = \frac{i+j}{n} \quad \text{Probability of } B = \frac{j+k}{n}$$

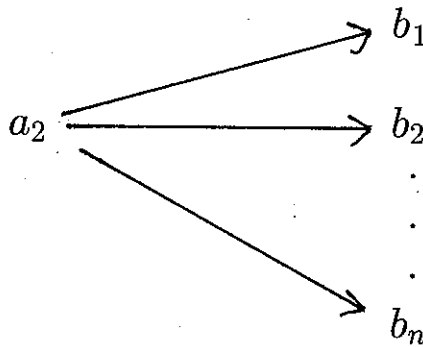
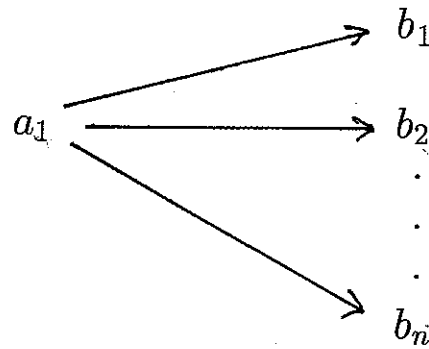
$$\text{Probability of } A \text{ and } B = \frac{j}{n}$$

$$\text{Probability of } A \text{ or } B = \frac{i+j+k}{n} = \frac{i+j}{n} + \frac{j+k}{n} - \frac{j}{n}$$

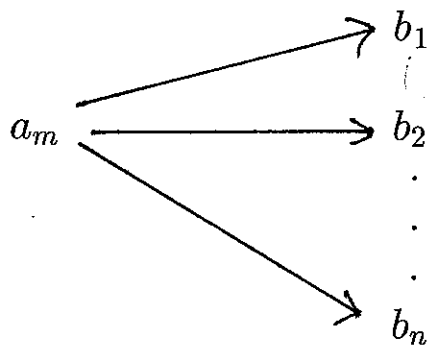
$$\text{Probability of } A \text{ or } B = \text{Probability of } A + \text{Probability of } B - \text{Probability of } A \text{ and } B$$

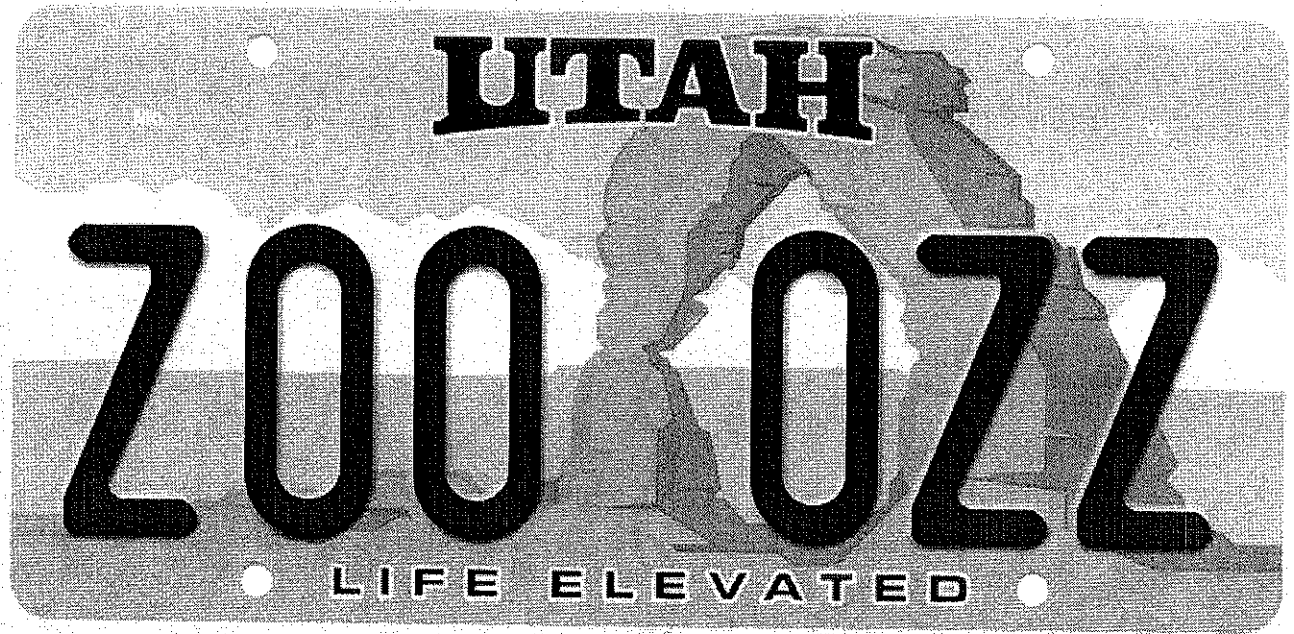
## FUNDAMENTAL COUNTING PRINCIPLE:

If event A can occur in  $m$  different ways and, after event A has occurred, event B can occur in  $n$  different ways, then there are  $m \cdot n$  possible ways for both events A and B to occur.



⋮





standard issue (1 version)

letter - number - number - number - letter - letter

(26) (10) (10) (10) (26) (26)

$\frac{10}{\quad} \cdot \frac{10}{\quad} \cdot \frac{10}{\quad} \cdot \frac{26}{\quad} \frac{26}{\quad} \frac{26}{\quad}$

numbers

letters

## Stat 1040

1. For a class of size 25, how many ways can you select a president, vice president, and secretary?
2. For a class of size 25, how many ways can you select a committee of three students?
3. Given  $n$  objects, how many ways can you select  $k$  of them?
4. Given 13 different letters, how many ways can you select 5 of them and arrange them in order?
5. What is the chance of winning the lottery?
6. Deron Williams makes 80 % of his free throws. What is the chance that he will make exactly 3 out of 5 free throws? 12 or more out of 15?

## Repeated Trials

1. From a class of 6 students, how many ways can you select a committee of size three?
2. From a class of 15 students, how many ways can you select a committee of size three?
3. How many ways can you fill in the blanks                          with exactly 3 H's and 2 T's?
4. Find the probability of getting exactly 3 *heads* in five tosses of a fair coin.

**Repeated Trials:** Suppose we have  $n$  independent trials, and the probability that event  $E$  occurs in any given trial is  $p$ . Then the probability that  $E$  will occur exactly  $k$  times is

$$\frac{n!}{k!(n-k)!} p^k (1-p)^{n-k}$$

5. Find the probability of getting exactly 3 *heads* in five tosses of a biased coin where the probability of heads is  $1/3$ .

6. A multiple-choice test has 10 questions, each with four choices. You are able to eliminate one of the choices on each question and then guess from the remaining 3 choices. A passing grade is to get 8 or more of the questions correct. Find the chance that you pass.

**Stat 1040**

1. How many ways can you select  $k$  objects from among  $n$  objects?

$$\text{"n choose k"} = \binom{n}{k} = \frac{n!}{k!(n-k)!}$$

[ Given  $n$  students, how many ways can you choose a committee of size  $k$  ? ]

2. Four draws are made with replacement from the box [ R , R , G , G , G , G , G ].

Find the probability that

- a) a red ticket is never drawn
- b) exactly 3 red tickets are drawn
- c) exactly 4 green tickets are drawn

3. A coin will be tossed 10 times. Find the probability of getting

- a) exactly 4 heads
- b) exactly 5 heads
- c) at least 2 heads

## PROBABILITY RULES ( The World )

**Definition:** The probability [chance] of event A is the proportion [percentage] of the time A is expected to happen when the random process is repeated over and over again.

**Opposite Event Rule:** The probability that event A happens is equal to one minus the probability that A doesn't happen.

**Multiplication Rule:** The probability that events A and B both happen is equal to the probability that A happens times the probability that B happens given that event A has occurred.

**Definition:** Two events are mutually exclusive when the occurrence of one prevents the occurrence of the other.

**Addition Rule:** The probability that event A or event B happens is equal to the probability that A happens plus the probability that B happens minus the probability that both happen. If events A and B are mutually exclusive, then the probability that event A or B happens is simply the sum of the probabilities.

**Definition:** Two events are independent if when one happens, the probability that the other happens is unchanged.

**Fundamental Counting Principle:** If event A can occur in  $m$  ways and after A occurs event B can occur in  $n$  ways, then the number of ways both events A and B can occur is  $m \times n$ .

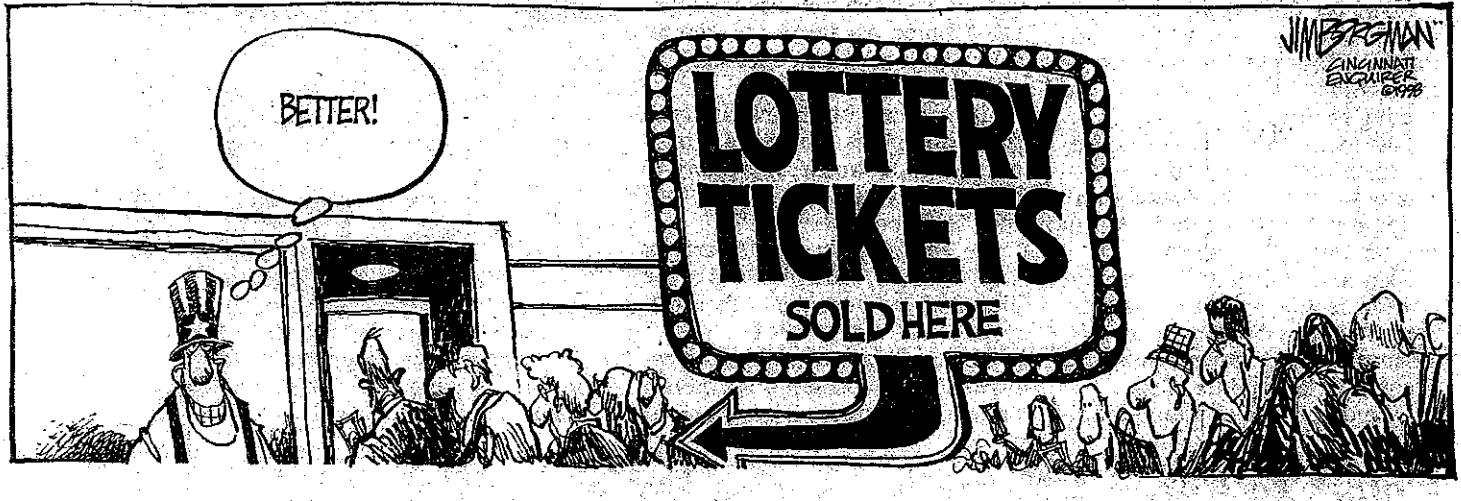
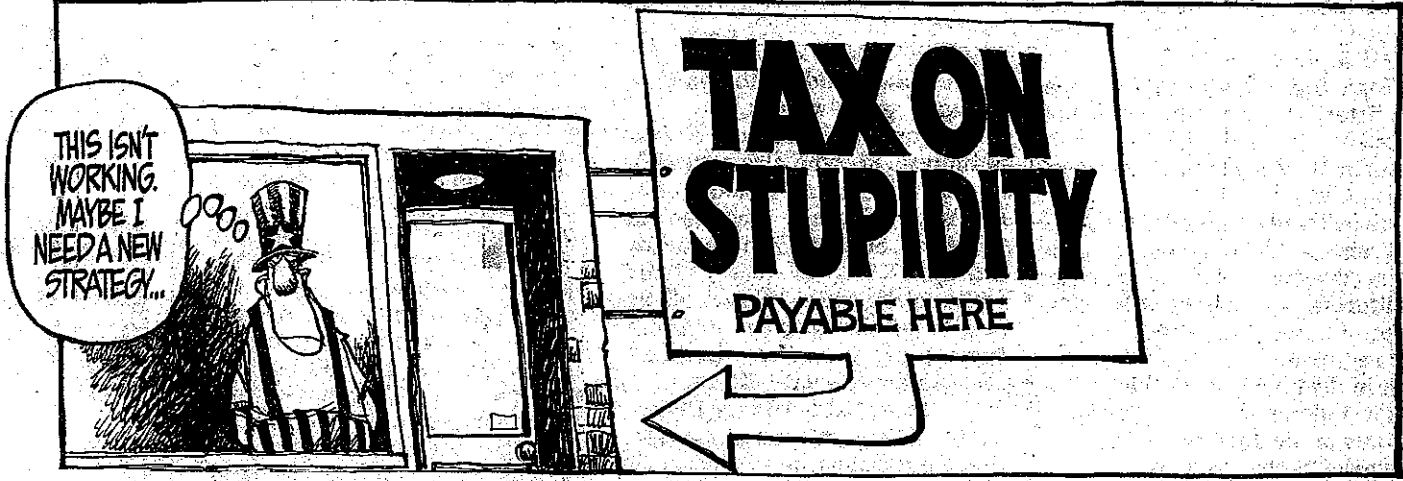
The number of ways  $k$  objects can be selected from  $n$  objects without regard to order is

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

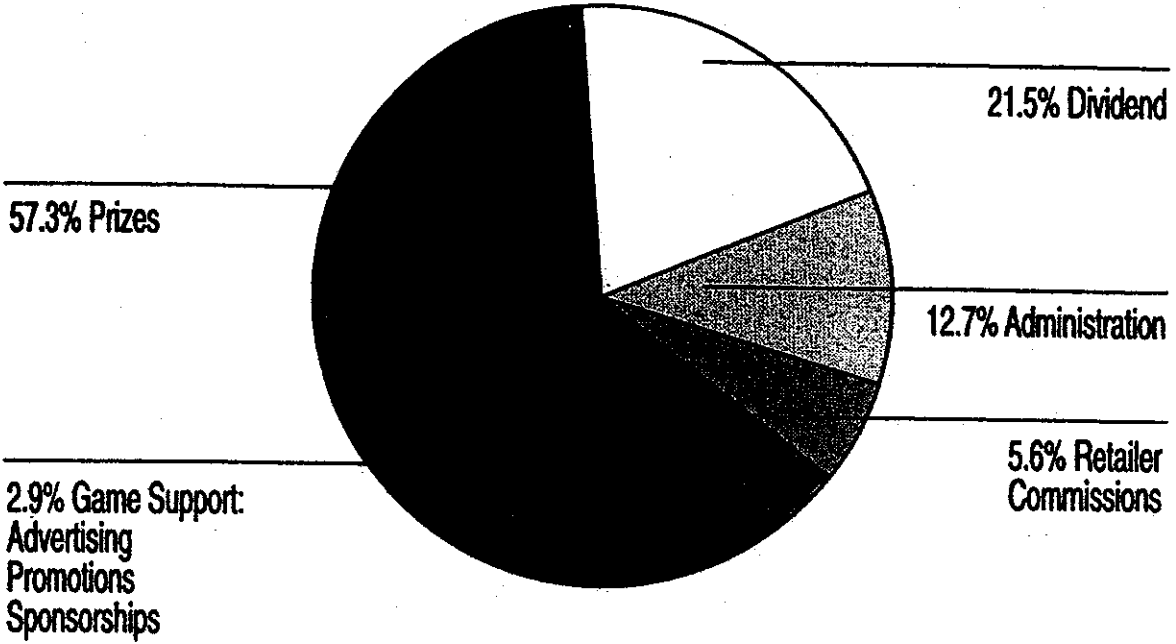
**Repeated Trials:** Suppose we have  $n$  independent trials, and the probability that event E occurs in a given trial is  $p$ . Then the probability that E will occur exactly  $k$  times is

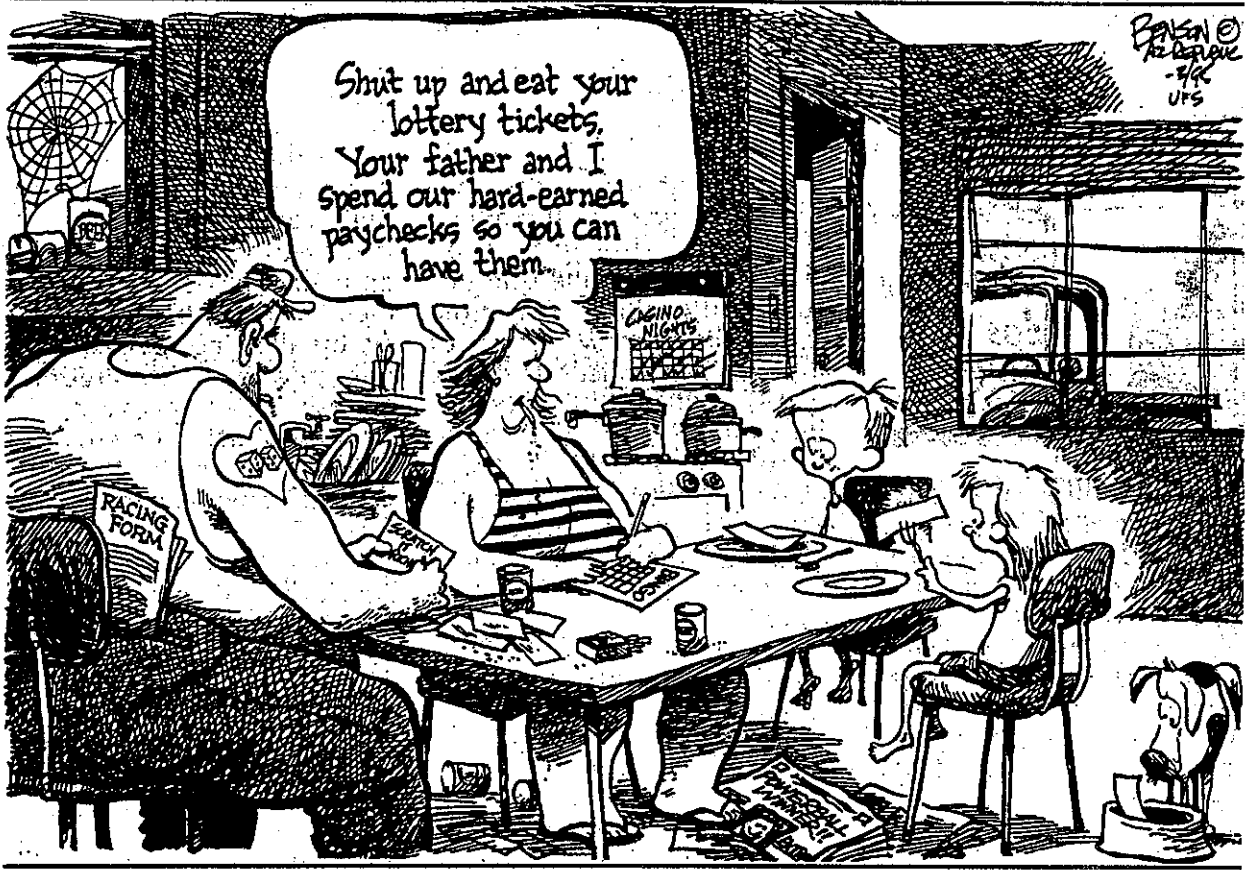
$$\frac{n!}{k!(n-k)!} p^k (1-p)^{n-k}$$





**EXPENDITURES BY STATUTORY CATEGORY**





B.C.

