8-26-14

MATH 4200 FOUNDATIONS OF ANALYSIS SYLLABUS

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Objectives: This course serves as a transition from the intuitive development of calculus to the more rigorous advanced calculus and analysis courses. After reviewing elementary logic and set theory, students will construct the real number system and then focus on the theory of limits and continuity. Emphasis is placed on understanding, constructing, and writing proofs. A historical perspective is also provided by considering some of the famous proofs, problems, and personalities in the history of mathematics.

Prerequisites: Math 2210, 2250; or 2210, 2270, 2280 (3F, Sp)

Textbook: *Introduction to Analysis 5th Edition,* Edward D. Gaughan, American Mathematical Society 2009. ISBN-978-0-8218-4787-9

Office Hours: 2:30 - 3:30 PM; T, Th in AnSci 306

| Examinations: | Test 1 | 100 points |
|---------------|--------|----------------------------|
| | Test 2 | 100 points |
| | Final | 200 points (comprehensive) |

Quizzes: Five quizzes will be given, each worth 20 points.

Assignments: Written assignments will be collected and a portion of each will be graded. Their total will be worth 100 points. Late assignments will not be accepted.

Grading Policy: Grades will be based on the 600 points indicated above. The following is an approximate grade distribution.

A: 30% B: 45% C: 20% D,F: 5%

Topics Covered:

1. Language and Proofs

Quantifiers and logical statements, negations, introduction to proofs, counting principles

2. Sets and Numbers

Notation and terminology about sets, set operations

3. Functions

Definitions and terminology, sequences, graphs, bijections, composition

4. Mathematical Induction

Axioms for the natural numbers, equivalent induction axioms, induction proofs, Fibonacci numbers

5. Counting and Cardinality Finite and infinite sets, countable and uncountable sets

6. Divisibility

Division algorithm, prime factorization theorem

- 7. Rational Numbers Equivalence relations, constructing the rationals, irrational numbers
- 8. Counting Principles and Recurrence Relations Binomial coefficients, pigeon hole principle,

9. Real Numbers

Completeness axiom, the Archimedean property, limits of sequences, monotone convergence theorem, decimal expansions, uncountability of R

10. Sequences and Series

Cauchy sequences, squeeze theorem, Bolzano-Weierstrass Theorem, harmonic series, tests for convergence

11. Continuity

Characterization of continuity, Intermediate Value Theorem, uniform continuity

12. Differentiation

Linear approximation theorem, derivative rules, Chain Rule, Mean Value Theorem

13. Integration

Definition of the integral, Fundamental Theorem of Calculus

Mathematics is the nuclear furnace of science. It is the crucible in which the fundamental ideas and concepts of science are created. It is for this reason that mathematics has been crowned the queen of the sciences ... It is difficult to define mathematics and one knows something about it only by doing it. Its enjoyment can only be experienced. It has many virtues. It enjoys the precision of science as well as the creative freedom of art. And if one listens carefully, one can hear its music as well. M. Ram Murty, Professor of Mathematics, McGill University