

Find all zeros of the polynomial  $V(x) = 2x^3 + x^2 - 18x - 9$ .

1. Possible rational zeros:  $\pm 1, \pm 9, \pm 3, \pm \frac{1}{2}, \pm \frac{9}{2}, \pm \frac{3}{2}$

2. Since  $V(3) = 54 + 9 - 54 - 9 = 0$ ,  $x - 3$  must be a factor.

3. Use long division to divide  $2x^3 + x^2 - 18x - 9$  by  $x + 3$ .

$$2x^3 + x^2 - 18x - 9 = (x + 3)(2x^2 - 5x - 3)$$

4. Now  $2x^3 + x^2 - 18x - 9 = (x + 3)(2x^2 - 5x - 3) = (x + 3)(x - 3)(2x + 1) = 0$

when  $x = -3$ ,  $x = 3$ , and  $x = -\frac{1}{2}$ .